

## **SYSTEM AND METHOD FOR DETERMINING PROPERTIES OF A TUBULAR CAVITY**

### **FIELD OF THE INVENTION**

The present invention relates to determining properties of a tubular cavity  
5 including the location of a device inserted into the cavity.

### **BACKGROUND OF THE INVENTION**

In many fields there is a need to determine information about the cavity of  
tubular structures, such as blood vessels or pipelines. This information can  
include the thickness of the walls, the maximum and minimum internal diameters,  
10 and the location of a device inserted into the cavity relative to the cavity.

In anatomy the cavities of such tubular organs (for example veins and  
arteries) are called lumens. A typical prior art solution for analyzing lumen  
geometry and navigating within them has been to use ultrasound. For example,  
in an ultrasound coronary investigation a full circle scan (2D) is used in order to  
15 estimate the lumen size of a blood vessel. To achieve the estimate requires a  
large amount of computational power and involves sophisticated image  
processing schemes.

The present invention proposes a simple method for determining lumen  
properties by analyzing signals from a device placed inside the lumen.

20 In summary, it is a main object of the present invention to provide a  
method for analyzing signals from a device inside a tubular cavity to determine  
properties of the cavity including the location of the device.

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The calculating power required for the present invention is significantly less than that required for conventional image processing methods, generally two orders of magnitude less.

Still further objects and advantages will become apparent from a  
5 consideration of the ensuing description and drawings.

**BRIEF DESCRIPTION OF THE INVENTION**

There is thus provided, in accordance with a preferred embodiment of the present invention, A computer based method for determining the distance of a transceiver located within a lumen from the center of the lumen and for  
10 determining the radius of the lumen, the lumen crosssection being substantially circular at the transceiver location, the method applied on data received from a transceiver placed at a position within the lumen that is distance (r) from the center and distance (a) from the lumen wall, transmitting a signal of known velocity (v) that can be correlated with the time of flight and  
15 receiving a first signal and a second signal that are reflections of the transmitted signal, timing the time differences between the transmission of the transmitted signal and reception of the first (t1) and second (t2) reflection signals, the method comprising:

- a. Calculating the distance of the transceiver from the center of the  
20 lumen =  $(t1 - t2)v/4$ ;
- b. Calculating the diameter of the lumen =  $(t1 + t2)v/2$ ;

**BRIEF DESCRIPTION OF THE FIGURES**

The invention is described herein, by way of example only, with reference to the accompanying Figures, in which like components are designated by like reference numerals.

5    FIG. 1    illustrates a model of the geometry of a lumen with a transceiver inside it.

FIG. 2    illustrates a model of the geometry of a lumen with a transceiver inside it taking into account angular reflections along the reflection direction

**DETAILED DESCRIPTION OF THE INVENTION**

10            The present invention proposes a simple method for determining lumen properties by analyzing signals from a device placed inside the lumen. The device is assumed to be a transducer and the signals are assumed to be ultrasound. However the signals can be any signal that can be correlated with its time of flight.

15            Ultrasound measurements consist of an emission of a sound at very high frequency, listening to the echo, and analyzing the echo structure. Blood vessel wall reflects ultrasound, thus enabling good distance measurement. Various components of the blood system reflect ultrasound waves as well, but with different efficiencies, i.e. intensities, noise, etc. The sum of those differences  
20            provide information about the blood vessel and the lumen.

              Ultrasound measurements comprise a simple procedure:

- Emission of a short pulse of acoustic energy
- Exact registration of the emission time
- "Listening" to echoes (multiple reflections)
- 25            - Electronic and mathematical signal manipulations

- Echo classification
- Distance (arrival time) estimates
- Display in terms of image and/or numbers.

5        Ultrasound is basically a pressure wave or wave packet and behaves according to simple laws of optics. We do not refer here to nonlinear effects like cavitations, frequency dispersion, etc.

Consequently, we can define our physical system as comprising a pulse source (ultrasound emitter), a nondispersive propagation medium, a cylindrical reflector and a receiver (ultrasound receiver). The reflector has two types of  
10    influence on the impinging waves:

- Reflection: like any other surface it reflects according to the geometry and impinging angles.
- Spatial dispersion: some energy will be reflected around the reflection angle, thus a Lambertian element will be present in the reflection  
15    pattern. (A Lambertian reflector is characterized by reflection intensity different from zero at angles other than reflection angle. The reflection pattern resembles a lobe shape oriented along the reflection direction. The more is the reflector Lambertian in nature, the more wide the pear shape will be. A perfect Lambertian reflector reflects light with equal  
20    intensity at all angles disregarding the direction of the impinging light.)

The system has a cylindrical symmetry, hence a plane model will suffice.

The mathematical equations are developed according to the following assumptions:

- Ultrasound source is a point and has a constant angular radiation  
25    pattern.
- Ultrasound receiver is a point and has a constant angular sensitivity pattern.

- Reflector is a circle with a perfectly reflecting mirrorlike surface.
- There is no intensity attenuation

The mathematical model is indeed very simple as only two algebraic equations are used. The geometry of the model is shown in FIG. 1. Lumen (circle)  
 5 10 has a radius ( $R$ ). Transceiver 12 (comprising a transmitter and a receiver, both having no effective spatial extension) is located at a distance ( $a$ ) from the lumen perimeter and at a distance ( $r$ ) from the center.

Within the framework of the model, waves are reflected from a specular surface according to the laws of geometric optics. The reflecting surface has a  
 10 circular shape. Waves emerging from the transmitter will bounce from the surface at equal angles with respect to the normal at the surface at the same point. Since normal lines at circle are passing through the center they are the same as diameters. Hence only reflections along the diameter passing through the transducer will reach the receiver. Hence, a receiver can detect only waves  
 15 coming from the peripheral points located along the line connecting the circle center and the detector. This line intersects the circle at two points. Only waves from these points will be detected by the receiver.

One wave is reflected by the near side and is received at a time given by

$$t_1 = \frac{2 \cdot (R - r)}{v} \quad (1)$$

20 where  $v$  is the sound velocity in the medium.

The second wave is reflected by the far side and is received at a time is given by

$$t_2 = \frac{2 \cdot (r + R)}{v} \quad (2)$$

Solving the two equations one has the distance between the transducer  
 25 (emitter and receiver)  $a$  and the reflector radius  $R$  as:

$$r = \frac{(t_1 - t_2) \cdot v}{4} \quad (3)$$

$$R = \frac{(t_1 + t_2) \cdot v}{4} \quad (4)$$

The two numbers given by equations (3) and (4) provide all the needed information:

5  $r$  – the location of the transducer within the circle.

$R$  – The circle radius

Thus, from a very simple measurement one can provide the "navigation" map in terms of path size and location on the path.

10 An assumption that can be discarded is the specular mirror nature of the reflector. A more realistic assumption is a surface that has some angular reflections along the reflection direction, i.e. it is Lambertian to some extension. This can be taken into account using the model in FIG. 2. The equations (1) and (2) must be modified to:

$$r \cdot \cos \theta + a \cdot \cos \alpha = R \quad (5)$$

$$15 \quad r \cdot \sin \theta = a \cdot \sin \alpha \quad (6)$$

After some simple calculations one finds:

$$a = \sqrt{R^2 + r^2 - 2 \cdot r \cdot R \cdot \cos \theta} \quad (7)$$

Equation (7) reflects the simple fact that for a variation of the angle  $\theta$  between 0 and 180°,  $a$  is monotonously increasing. The significance is crucial:

20 The arrival time of every reflection is correlated to the reflection geometry. From the point of view of the mirror model this means that all the reflections from other points not on the center-to-transducer line will reach the transducer at times between  $t_1$  and  $t_2$  in an ordered manner.

One should mention that a secondary reflection traveling twice the diameter can be detected. Time of flight is precisely fourtimes the result in eq. (4). The numerical result is independent of the transducer position inside the lumen.

- 5        If one assumes a narrow Lambertian distribution around the reflection angles, then only the small angles reflections will significantly contribute to the line widths.

Another factor to be taken into account is the optical distortion caused by large field of view in the case where the receiver and transmitter are not the  
10       same mathematical point). This effect will contribute to some line widening.

Calculated ultrasound signal shows clearly that the main contribution is connected to the line width.

It should be clear that the description of the embodiments and attached Figures set forth in this specification serves only for a better understanding of the  
15       invention, without limiting its scope.

It should also be clear that a person skilled in the art, after reading the present specification could make adjustments or amendments to the attached Figures and above described embodiments that would still be covered by the scope of the present invention.